# Accurate assessment of the Hirakud smelter aluminium reduction cell thermal balance using only temperature measurements

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### ABSTRACT

In the present study, the heat balance of the Hirakud smelter aluminium reduction cell has been accurately assessed using only a surface thermocouple and a pyrometer. As it is well known that using a single linear or quadratic relationship to estimate the heat flux from the measured surface temperature does not provide the accuracy required to close the cell heat balance, this approach was not used in this study.

Instead, the fundamental natural convection and radiation heat flux equations were used systematically for each measurement point. Practically, this means that the ambient air temperature and at least one ambient radiative temperature must also be known in addition to the surface temperature for each measurement point. Sometimes, the radiative heat flux could not be accurately estimated using a single ambient radiative temperature. In those cases, a more accurate estimation based on two ambient radiative temperatures and corresponding view factors has been used instead.

It turns out that although at least three temperature measurements are required to estimate a single heat flux, it takes a lot less time to make those temperature measurements using a pyrometer than directly measuring the heat flux using an expensive heat flux meter. Furthermore, no loss in accuracy was detected when using this approach as the cell heat balance could be closed within 5%, the level of accuracy typical of cell heat balance assessment using heat flux meter.

### **INTRODUCTION**

In his paper "Pot Heat Balance Fundamentals", Bruggeman [1] wrote as introduction: "The heat balance is not only a focal point for the economics of production, but also for the science of aluminum production". He also added: "By the end of the 1960's, correlation and simple mathematical models harnessing the power of early computers were available to improve cell design. Since then, both measurement methods and models have advanced further to the point where, new designs are not considered without rigorous testing and screening using these sophisticated tools".

So obviously, the first priorities of the Hirakud smelter cell retrofit program has been to measure the cell heat balance and to develop reliable mathematical models. The present paper focuses on the work done to assess the thermal balance of the cell.

### THE CELL HEAT BALANCE

The concept of the cell heat balance is quite simple. Of the total electrical power fed to the cell, less than half is actually used to produce aluminium. The remaining part must be dissipated as heat losses by the cell in order for it to maintain its thermal equilibrium. Experimentally, a cell voltage break down is required in order to calculate the cell internal heat i.e. the heat that the cell needs to dissipate to maintain its thermal equilibrium. In turn, this can be experimentally confirmed by directly measuring the cell heat losses. If the cell heat losses correspond to the calculated cell internal heat, those measurements can be used with confidence in order to calibrate the mathematical models of the cell.

### HEAT LOSSES MEASUREMENT METHODS

In general, cells loose heat by natural convection and by radiation. The equations that describe the physics of those two heat transfer mechanisms are well known. In the early cell heat balance measurement campaigns, those equations were indirectly used to compute the heat fluxes on the different cell surfaces and hence to compute the total cell heat losses [2]. They were only used indirectly probably because of the limitation of the computing power at that time: the fundamental equations were used to correlate the different cell surface temperatures to the heat fluxes (see Figure 1 extracted from [2]). Those correlations were established in preparation for the actual field measurement campaign in order to reduce it to the measurement of the cell surface temperatures only. This approach turned out not to produce very accurate results.



Figure 1: Relation between surface temperature and heat dispersion (Fig 6 in [2])

Very recently [3], those same fundamental equations have been presented again as background theoretical knowledge, but the authors carefully specified that: "Due to geometry and other conditions of an electrolysis cell, (those) equations cannot be used directly for (calculating) the heat flow from shell wall to air".

In [1], Bruggeman clearly expressed the current conventional wisdom of the industry by specifying that heat flux transducer must be used to carry out cell heat loss measurement campaigns. He even pointed out that: "Haupin developed a heat flux transducer especially for pot measurements". Apart from Alcoa, most of the rest of the industry is rather using commercially available heat flux transducers (see Figure 2).



Figure 2: Commercially available heat flux transducers (<u>www.kyoto-kem.com</u>)

Unfortunately, commercially available heat flux transducers are fairly expensive and relatively fragile. They are also characterized by a fairly long response time of around 10 minutes. This means that cell heat balance measurement campaigns using heat flux transducers are fairly long and expensive to carry out. For that reason, the challenge posed to the authors was to find an accurate way to assess the Hirakud cell thermal balance using only temperature measurements.

### FUDAMENTAL HEAT FLUX EQUATIONS

The general form of the heat transfer equations have been published multiple times, references [2,3] being two examples. But as the natural convection heat loss equations are semi-empirical, there exact form varie from author to author. In the present work, we used the following equations to compute the heat fluxes [4]:

$$q_{tot}(W/m^2) = q_c + q_r \tag{1}$$

$$q_c(W/m^2) = Nu \cdot \frac{k}{L} \cdot (T_s - T_A)$$
<sup>(2)</sup>

$$q_r(W/m^2) = \varepsilon \sigma \left( (T_s + 273)^4 - (T_o + 273)^4 \right)$$
(3)

For vertical surfaces, we have:

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$$Nu = 0.59 Ra^{\frac{1}{4}}, \text{ for } 10^4 \le Ra \le 10^9$$
 (4)

$$Nu = 0.105Ra^{\frac{1}{3}}, \text{ for } 10^9 \le Ra \le 10^{12}$$
(5)

For horizontal surfaces facing up we have:

$$Nu = 0.54 Ra^{\frac{1}{4}}, \text{ for } 10^5 \le Ra \le 2 \times 10^7$$
 (6)

$$Nu = 0.141Ra^{\frac{1}{3}}$$
, for  $10^7 \le Ra \le 10^{11}$  (7)

And finally, for horizontal surfaces facing down we have:

$$Nu = 0.27 Ra^{\frac{1}{4}}, \text{ for } 3 \times 10^5 \le Ra \le 3 \times 10^{10}$$
(8)

Where:

$$Ra = \frac{g\beta L^3 (T_s - T_A)}{v^2} \cdot \Pr$$
(9)

In order to be able to evaluate equations (2) and (9), we need to know the value of k, v and P<sub>r</sub> at T<sub>f</sub>, the air film temperature:

$$T_f = \frac{\left(T_s + T_A\right)}{2} \tag{10}$$

Those air properties are presented in Table 1 [4]:

### Table 1

Property values of air at atmospheric pressure

T (°C)	k (W/m °C)	v (m2/s)	Pr
27	0.02624	1.5680E-05	0.70757863
77	0.03003	2.0760E-05	0.69613541
127	0.03365	2.5900E-05	0.68883717
177	0.03707	3.1710E-05	0.68391149
227	0.04038	3.7900E-05	0.68102827
277	0.04360	4.4340E-05	0.67880692
327	0.04659	5.1340E-05	0.68353418
377	0.04953	5.8510E-05	0.68218017
427	0.05230	6.6250E-05	0.68508023
477	0.05509	7.3910E-05	0.68584970
527	0.05779	8.2290E-05	0.68859443
577	0.06028	9.0750E-05	0.69301739
627	0.06279	9.9300E-05	0.69595557
677	0.06525	1.0820E-04	0.69760123
727	0.06752	1.1780E-04	0.70194124
827	0.07320	1.3860E-04	0.70372446
927	0.07820	1.5910E-04	0.70689900
1027	0.08370	1.8210E-04	0.70496393

Finally, by fitting the data of Table 1 with 4 order polynomials, we can establish the following equations for the air thermal conductivity, the air cinematic viscosity and the air Prandtl number respectively:

$$k = 2.014E - 15 \times T_f^4 + 1.68E - 11 \times T_f^3 - 4.118E - 8 \times T_f^2 + 8.051E - 5 \times T_f + 0.02407$$
(11)

$$v = 1.438E - 17 \times T_f^4 - 3.25E - 14 \times T_f^3 + 9.095E - 11 \times T_f^2 + 8.977E - 8 \times T_f + 1.32E - 5$$
(12)

$$Pr = 1.937E - 13 \times T_f^4 - 6.581E - 10 \times T_f^3 + 7.349E - 7 \times T_f^2 - 2.788E - 4 \times Tf + 0.714$$
(13)

Equations (1) to (13) define a close form function that can be summarized as:

$$q_{tot}(W/m^2) = F_q(T_s, T_A, T_O, \mathcal{E}, L, SO)$$
(14)

Where:

- $T_{S}$  (°C) is the measured surface temperature
- $T_A$  (°C) is the measured air temperature close to the surface
- $T_O$  (°C) is the measured facing radiative background temperature
- ε is the surface emissivity
- L (m) is the surface typical length
- SO is the surface orientation (V, OH or OD)

### **MEASUREMENT CAMPAIGN**

In order to calculate the global cell heat losses, approximately 200 surfaces must be established around the cell. The area of each of those surfaces must be calculated in order to be able to, in turn, calculate the heat dissipated by each of them:

$$Q_i(W) = A_i \cdot F_q(T_s, T_A, T_O, \varepsilon, L, SO)_i$$
<sup>(15)</sup>

$$Q_{cell}(kW) = \sum_{1}^{N} Q_i / 1000$$
(16)

The actual implementation of this approach is not as complex as it may look. It is quite easy to evaluate ahead of time A,  $\varepsilon$ , L and SO for each surface. For a given cell design, once established, the value of those items will not change. This leaves only three temperatures to be measured per surface  $T_S$ ,  $T_A$  and  $T_O$  during the measurement campaign.

In comparison, in a "standard" measurement campaign using heat flux transducers, only  $q_{tot}$  is measured for each surface. Yet, measuring  $T_S$  and  $T_O$  with a small hand held pyrometer and  $T_A$  with a thermocouple and a small hand held multimeter is far less cumbersome and requires far less time than using slow to response heat flux transducers connected by wires to an expensive and delicate heat flux meter!

### **ANALYSIS OF THE RESULTS**

Despite all the theoretical and advance preparation work, there were no guarantees that this new measurement approach would produce accurate results. In fact, our first attempt did not; the measured heat losses significantly exceeded the calculated cell internal heat!

Analysis of the results revealed that we were overestimating the heat flux of some very hot surfaces for which the radiation term became very large. Of course, we knew that the radiative exchanges around a cell are very complex and that considering that each surface is only seeing one background radiative temperature could well turn out to be an unrealistic over-simplification. Our first results confirmed that this was the case, at least for some critical surfaces.

This led us to consider that those surfaces are seeing two background radiative objects that are not at the same temperature. Of course, this in turn introduce the need to calculate the view factors for each object:

$$q_r(W/m^2) = \varepsilon \sigma \Big[ F \Big( (T_s + 273)^4 - (T_o + 273)^4 \Big) + (1 - F) \Big( (T_s + 273)^4 - (T_o + 273)^4 \Big) \Big]$$
(17)

In a second attempt, we use this new equation to evaluate the radiative heat transfer of the few regions of the cell were hot surfaces are partially seeing another hot surface. This second time, the percentage of closure was in the acceptable rage as we can see in Table II. A third attempt, which was also successful, on a different cell confirmed that we had developed an accurate method to assess the thermal balance of the Hirakud cell using only temperature measurements.

## Table II

#### Heat Balance Results

date:	5-Nov-03	Cell:	Cell 265	
Cathode Heat Losses		W / m2	kW	<u>0</u> 0
Shell side	coverplate	821	2.26	2.00
Shell side	spacer between boxes	1796	3.59	3.18
	bottom box	3105	6.41	5.69
Collector bars to air		1337	7.96	7.06
Collector 1	bars to flexible		2.40	2.13
Shell side	wall collector bar level	625	0.57	0.50
Shell side	wall insulation level	981	1.80	1.60
Shell side	vertical boxes	918	1.97	1.75
Shell side	floor perimeter section	1172	9.56	8.48
Shell side	floor center section	1884	8.14	7.22
Shell end	coverplate	809	2.21	1.96
Shell end	spacer between boxes	1789	3.55	3.15
Shell end l		3065	6.29	5.58
Shell end	wall collector bar level	623	0.81	0.72
Shell end	wall insulation level	969	1.82	1.61
Shell end	vertical boxes	1150	2.16	1.92
Shell end	floor perimeter section	1165	6.34	5.62
Total for	the cathode part		67.82	60.17
Anode Heat	Losses			
Crust		306	2.85	2.53
First side	channel	4002	12.11	10.74
Second sid		2037	6.16	5.47
Third side		1206	3.65	3.24
Forth side	channel	739	2.24	1.98
Above fort	h side channel	554	1.70	1.51
Anode top		552	4.13	3.67
Studs			12.06	10.70
Total for	the anode part		44.9	39.83
10001 101			,	
Total for	the cell		112.7	100.00
Cell inter Blitz clos			117.8 95.71%	
	5		55.720	

### CONCLUSIONS

The heat balance of the Hirakud smelter aluminium reduction cell has been accurately assessed using only a surface thermocouple and a pyrometer. No loss in accuracy was detected when using this approach as the cell heat balance could be closed within 5%, the level of accuracy typical of cell heat balance assessment using heat flux meter.

Furthermore, it turns out that although at least three temperature measurements are required to estimate a single heat flux, it takes a lot less time to make those temperature measurements using a pyrometer than directly measuring the heat flux using an expensive heat flux meter.

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